

# Parallel Matlab Computation for STAP Clutter Scattering Function Estimation and Moving Target Estimation \*

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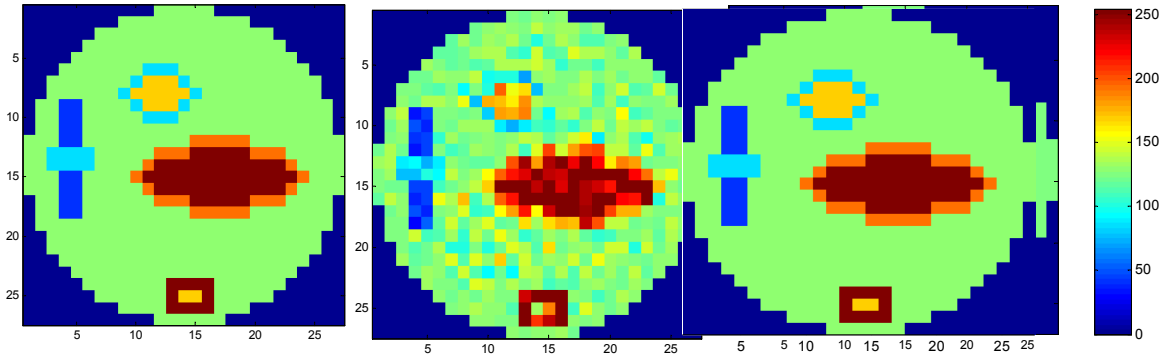
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## Abstract

Conventional moving target estimation in STAP radar applications is based, in part, on adaptive clutter scattering function estimation techniques. These techniques classically rely on radar return data from adjacent range gates to estimate the clutter scattering function for the range gate of interest. Here, we are interested in using geographical information systems in conjunction with accurate platform positioning information as the basis for the clutter scattering function estimation. The goal is to improve the effectiveness of moving target estimation techniques by providing additional information to the decision-making process.

Our problem formulation is consistent with the model for space-time adaptive processing (STAP) presented in [1]. A pulse-Doppler radar platform with multiple transmit/receive elements emits several pulse train along an arbitrary flight path, such as a circle around the region of interest. Each pulse train is assumed to be perfectly coherent within one coherent processing interval (CPI), but different pulse trains are assumed noncoherent with respect to one another. The ground region is subdivided into pixels, or ground patches. The range and angle of each ground patch with respect to the platform for each transmitted pulse is assumed known, along with the illumination pattern. The received data for one pulse is modeled as the sum of the returns from all of the ground patches, each modulated by the transmit illumination. The data from all pulses or viewpoints is modeled in this way. Maximum-likelihood methodology is used to estimate the unknown scattering function [2] and a variant of the Adaptive Matched Filter [3] is used for moving target estimation.



**Figure 1: Artificial scattering function example. True scattering function, estimated scattering function, and estimated with land-use aggregation.**

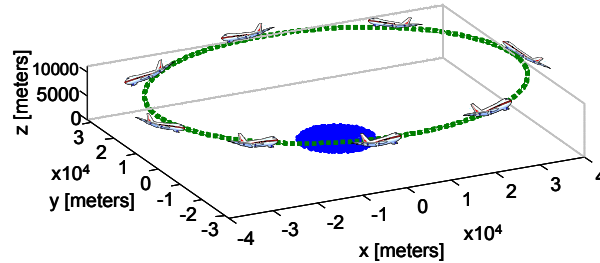
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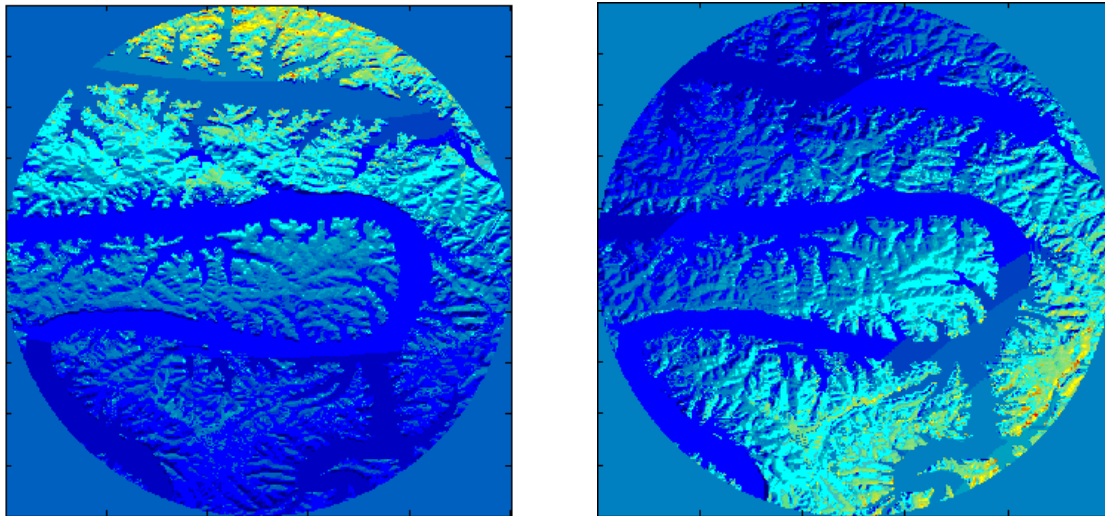
Figure 1 illustrates the scattering function estimation. This is an artificially low-dimensional simulation in which there are 550 ground patches, each associated with one of 9 different land-use values. The land-use value determines the clutter scattering function in each ground patch.

In the data collection scenario the radar platform moves in a circular flight path around the region of interest, as illustrated in Figure 2. The left panel of Figure 1 shows the true scattering function, the middle panel shows the estimated scattering function when the land use is not assumed known, and the right panel shows the estimated scattering function when pixels with the same land-use are assumed to have the same scattering function value (we call this land-use aggregation).



**Figure 2: Simulated flight pattern for artificial scattering function example**

An important question that arises is the assessment of the computational requirements associated with this application as the data set is scaled up to realistic sizes. To investigate this issue, a 15 km radius region centered on the Lake of the Ozarks in central Missouri is used as a full data set test case. With a pixel (ground patch) dimension of approximately 30 m, the region of interest comprises about 200,000 pixels. Figure 3 shows the illumination pattern on the ground for the full data set from a pair of looks. The digital terrain elevation map comes from a publicly-available website operated by the U.S. Geological Survey [4].



**Figure 3: Illumination of full data set from different looks.**

Our current activities include the execution of clutter scattering function estimation and moving target estimation on the full dataset illustrated above. The scattering function is based on 21 classes of land cover provided by the geographic information system. Given the large memory requirements for each look (greater than 250 MB/look); the computations are being executed in parallel (using MatlabMPI [5]) across 9 processors in a master-slave arrangement. The master processor is responsible for overall

coordination of the computations, and the 8 slave processors are each responsible for an individual look. We will present quantitative performance measurements on these parallel computations, including parallel efficiency as well as quality of results on the clutter scattering function and moving target estimates.

- [1] J. Ward. Space-time adaptive processing for airborne radar. MIT Lincoln Laboratory Technical Report 1015, December 1994.
- [2] D. Fuhrmann and L. Boggio. Radar imaging from multiple viewpoints and multiple noncoherent data sets. In *Proc.2004 Conf. Information Science and Systems*, Princeton University, Princeton, NJ, March 2004.
- [3] F. Robey, D. Fuhrmann, E. Kelly, and R. Nitzberg. A CFAR adaptive matched filter detector. *IEEE Trans. Aerospace and Electronic Systems*, vol. 28, no. 1, pp. 208-206, January 1992.
- [4] The National Map Seamless Data Distribution System, <http://seamless.usgs.gov>
- [5] Jeremy Kepner. Parallel Programming with MatlabMPI, In *Proc. of High Performance Embedded Computing Workshop*, September 2001.



Washington University in St. Louis

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# **Parallel Matlab Computation for STAP Clutter Scattering Function Estimation and Moving Target Estimation**

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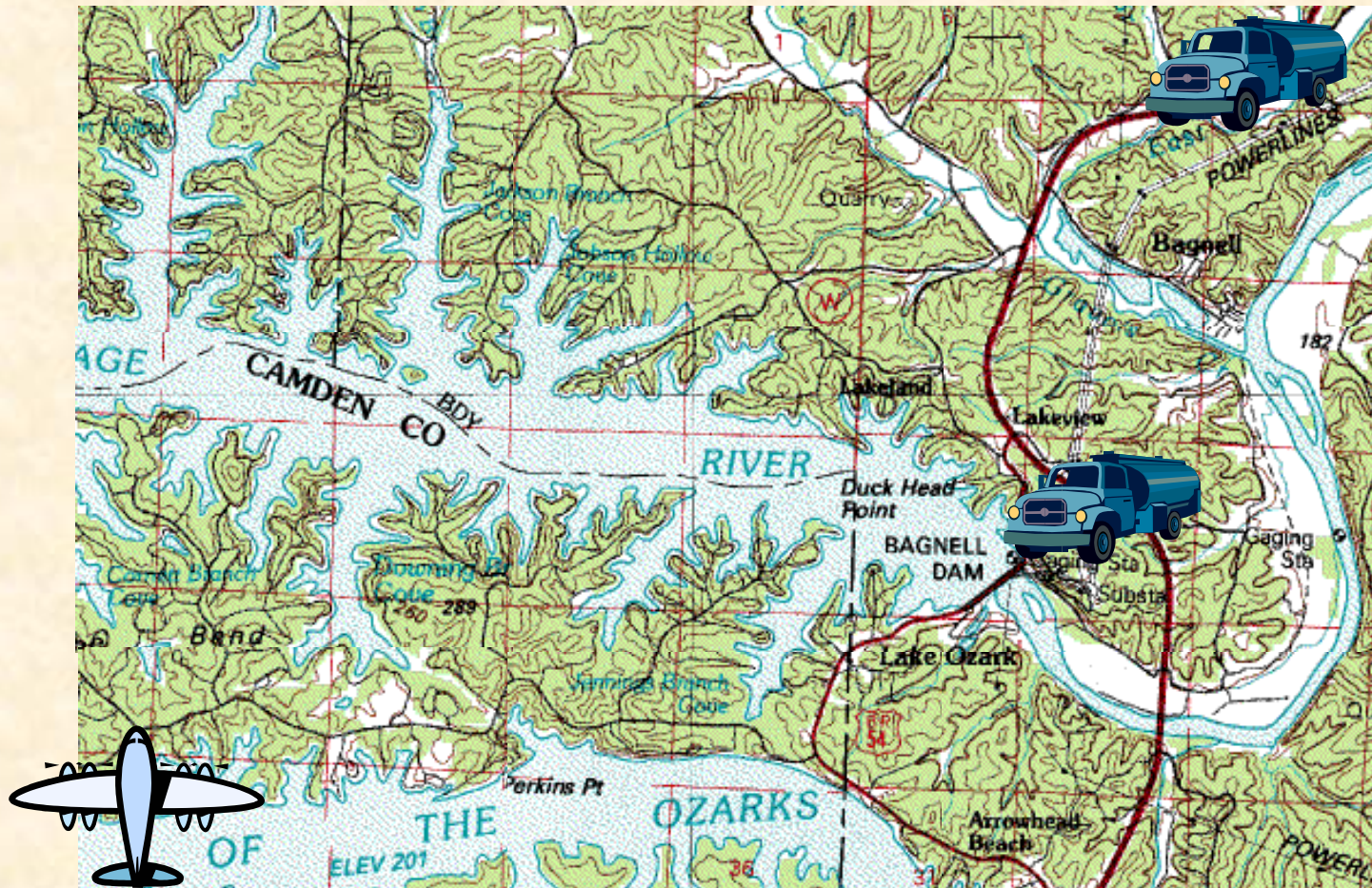
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Washington University in St. Louis**

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# Context



**Problem:** Detect ground moving targets  
in the presence of ground clutter

# Context

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- Wide-area surveillance airborne radar
- Arbitrary flight path
- Multiple sensors and Doppler pulses
- Space-time adaptive processing (STAP)
  - Better knowledge of the clutter covariance matrix gives better detection performance

**Objective:** Estimate the clutter covariance matrix and detect moving targets

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# Approach

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- Ground subdivided into pixels or ground patches
  - Known range and angle of each patch with respect to airborne platform
  - Known illumination pattern
  - Received data: sum of returns from targets and all patches on the ground
  - Prior knowledge is available:
    - Digital Terrain Elevation Maps
    - Land use information
-

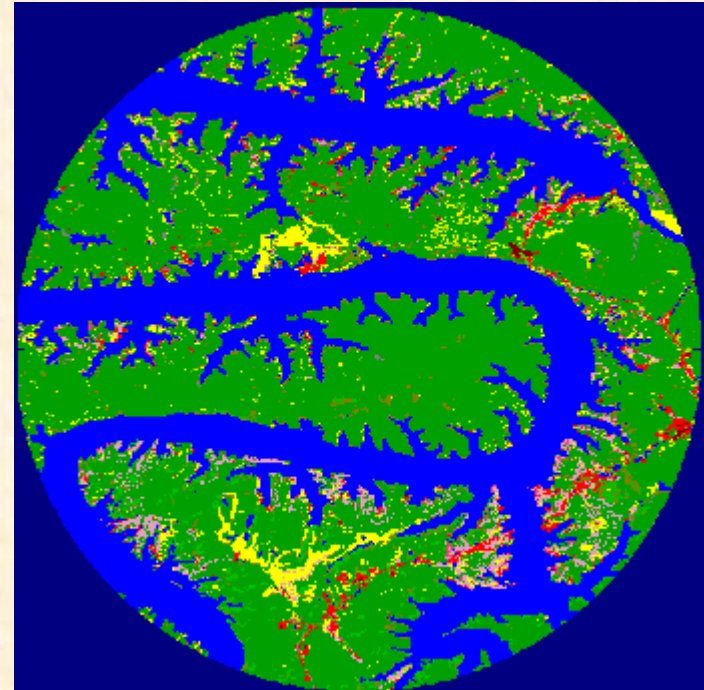


# Terrain Simulation

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- **Region of Interest**

- Lake of the Ozarks
- 15 km diameter
- 197,316 pixels
- 30m resolution



# Datasets

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- Obtained from USGS Seamless Data Server
    - 30m resolution
  - Digital Elevation Model
    - Used for modeling geometry
  - Land Use
    - Scattering function based on 21 classes of land cover
      - 9 primary classes
        - Water, Developed, Barren, Forested Upland, Shrubland, Non-Natural Woody, Herbaceous Upland Natural/Semi-natural Vegetation, Herbaceous Planted/Cultivated, Wetlands
      - Each class contains one or more categories, e.g.
        - Open Water, High-Intensity Residential, Deciduous Forest, Row Crops
    - Scattering function chosen arbitrarily for simulation
-

# Coordinate Systems

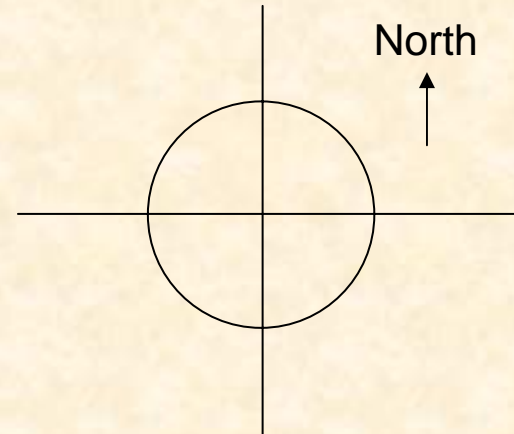
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- Datasets referenced in spherical coordinates
    - Latitude, Longitude, Elevation
  - Convert to Cartesian Coordinates
    - Simpler to use over small region
    - Computations can be made independent of Earth model
-

# Coordinate Conversion

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- First Stage
  - Origin at Earth's center
  - Use Geodetic Reference System 1980 (GRS80)
- Second Stage
  - Move origin to center of region of interest
  - Elevation along Z-axis
  - North along positive Y-axis

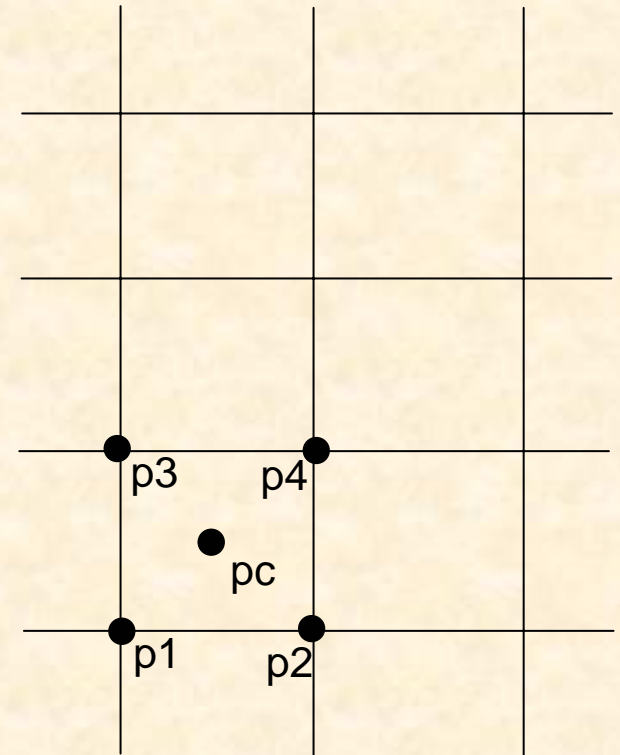




# Coordinate Systems

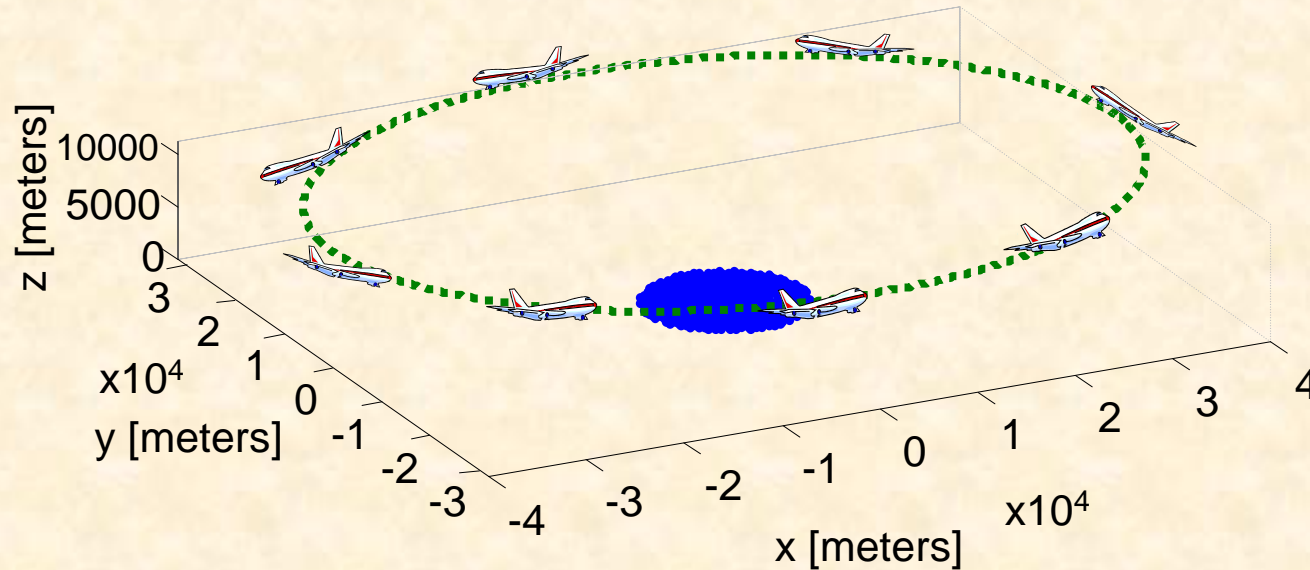
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- Adjacent data samples grouped into patches
  - Each patch, or pixel, contains:
    - Location for each corner
    - Location of center
    - Scattering function
    - Normal vectors
- 197,316 pixels in all



# Simulation Setup

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- Platform moves around region of interest
    - Actual flight path is arbitrary
  - Eight looks
-

# SIMULATION PARAMETERS

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- Platform
    - Flies in circular path around region
    - Radius 25 km
    - Altitude 7 km
    - 8 different viewpoints
  - Radar
    - $f_c$ : 10 GHz
    - BW: 10 MHz
    - PRF: 2 KHz
    - Pulses per CPI: 38
    - ULA elements: 12
    - Range gates: 990
-

# Geometry Parameters

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- Geometry dependent parameters required for simulation
    - Range to each pixel
    - Projected area of each pixel
      - Incident energy incorporates range and projected area of patch
    - Occluded pixels
      - Patches hidden from radar are removed using Z-buffer algorithm
        - Patches sorted by distance from radar
        - Any patch facing backwards or directly behind another is removed
    - Angle between platform's velocity vector and line of sight to each pixel
-



# Datacube Generation

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- Received data from a single patch

Return from  $n^{\text{th}}$  path is a random variable

$$u_k(n) \sim \mathcal{CN}(0, \lambda_k(n)\sigma_n)$$
$$\mathbf{z}_k = \mathbf{s}_k + \mathbf{n}_k + \sum_{n=1}^N u_k(n) \mathbf{a}_k(n)$$

return from targets

receiver noise

$$\mathbf{n}_k(n) \sim \mathcal{CN}(0, \epsilon \mathbf{I}_M)$$

Radar response vector

The diagram illustrates the equation for the received data vector  $\mathbf{z}_k$ . The equation is  $\mathbf{z}_k = \mathbf{s}_k + \mathbf{n}_k + \sum_{n=1}^N u_k(n) \mathbf{a}_k(n)$ . Annotations include: 

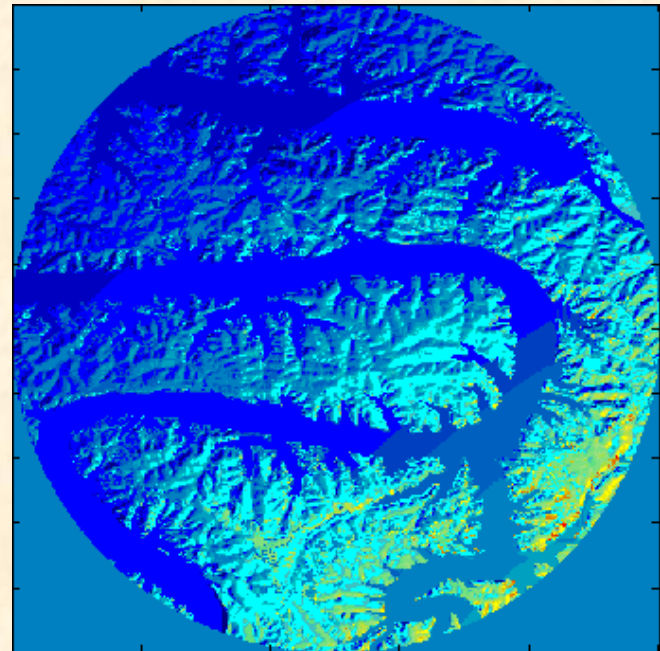
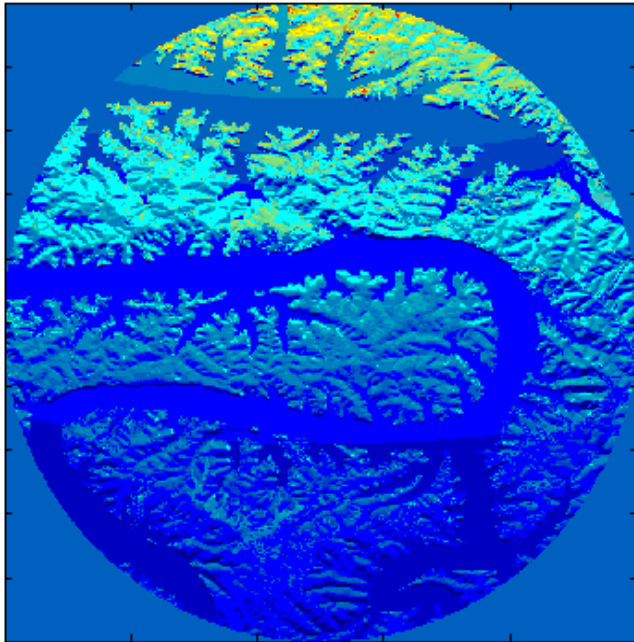
- An arrow from  $\mathbf{s}_k$  pointing to the text 'return from targets'.
- An arrow from  $\mathbf{n}_k$  pointing to the text 'receiver noise'.
- An arrow from  $u_k(n)$  pointing to the text 'Return from  $n^{\text{th}}$  path is a random variable' and another arrow pointing to the equation  $u_k(n) \sim \mathcal{CN}(0, \lambda_k(n)\sigma_n)$ .
- An arrow from  $\mathbf{a}_k(n)$  pointing to the text 'Radar response vector'.
- An arrow from  $\mathbf{n}_k(n)$  pointing to the equation  $\mathbf{n}_k(n) \sim \mathcal{CN}(0, \epsilon \mathbf{I}_M)$ .

- Response at a single range gate
    - Sum over all patches in range gate
-

# ILLUMINATION

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Illumination from different looks



# Scattering Function Estimation

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- Prototype designed and tested first
    - Implements EM algorithm
    - Uses a Small-Scale Dataset with 554 pixels
  - EM algorithm requires response vector for each pixel, in each look
    - For Small-Scale Simulation
      - 2,020,992 complex doubles
      - 30.8 MB of data
  - Large-Scale Simulation contains 197,316 pixels
    - 719,808,768 complex doubles
    - 10.73 GB
-

# Memory Reducing Techniques

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- Maintain only the Doppler and spatial vectors
    - Compute Kronecker product as needed
    - Reduces requirements to 1.17 GB
  - Lookup Table
    - Finely sampled table containing Doppler and spatial vectors
    - Indexed by a single value
    - Further reduces memory requirements
      - 10.64 MB when using a 10,000 entry table
-



# The Need For Parallelism

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- The EM Algorithm can be parallelized in multiple ways
    - Across looks
    - Across range gates
  - Parallelism improves the algorithm
    - Significant speedup in processing time
    - Additional physical memory available
      - Only 150 MB needed per look for the response vectors (250 MB when all other necessary data are included)
    - More effective cache
      - Possible gain when using a Lookup Table
-

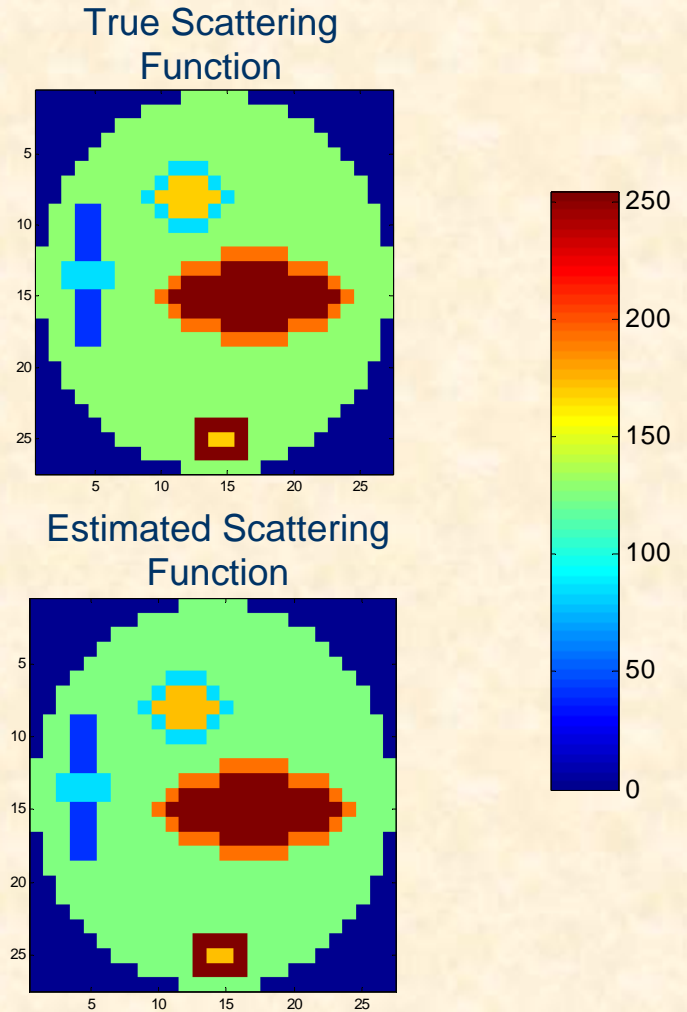
# Parallelism Using MatlabMPI

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- MatlabMPI provides parallel interface
    - Allows passing of messages between multiple systems that share a file system
  - Use 9 parallel threads (1 master, 8 slaves)
    - Slaves perform iterations of the EM algorithm on a single look
    - Master provides slaves with data and collects results from each iteration
  - Messages only sent at beginning and end of each iteration
-

# Results

- Small-Scale Simulation
  - Provides results identical to prototype version
  - Runs 4% slower than non-parallel version
    - Computation for a single look is too fast to gain from parallelism
    - Message passing overhead too large
    - Not a problem for full-scale simulation



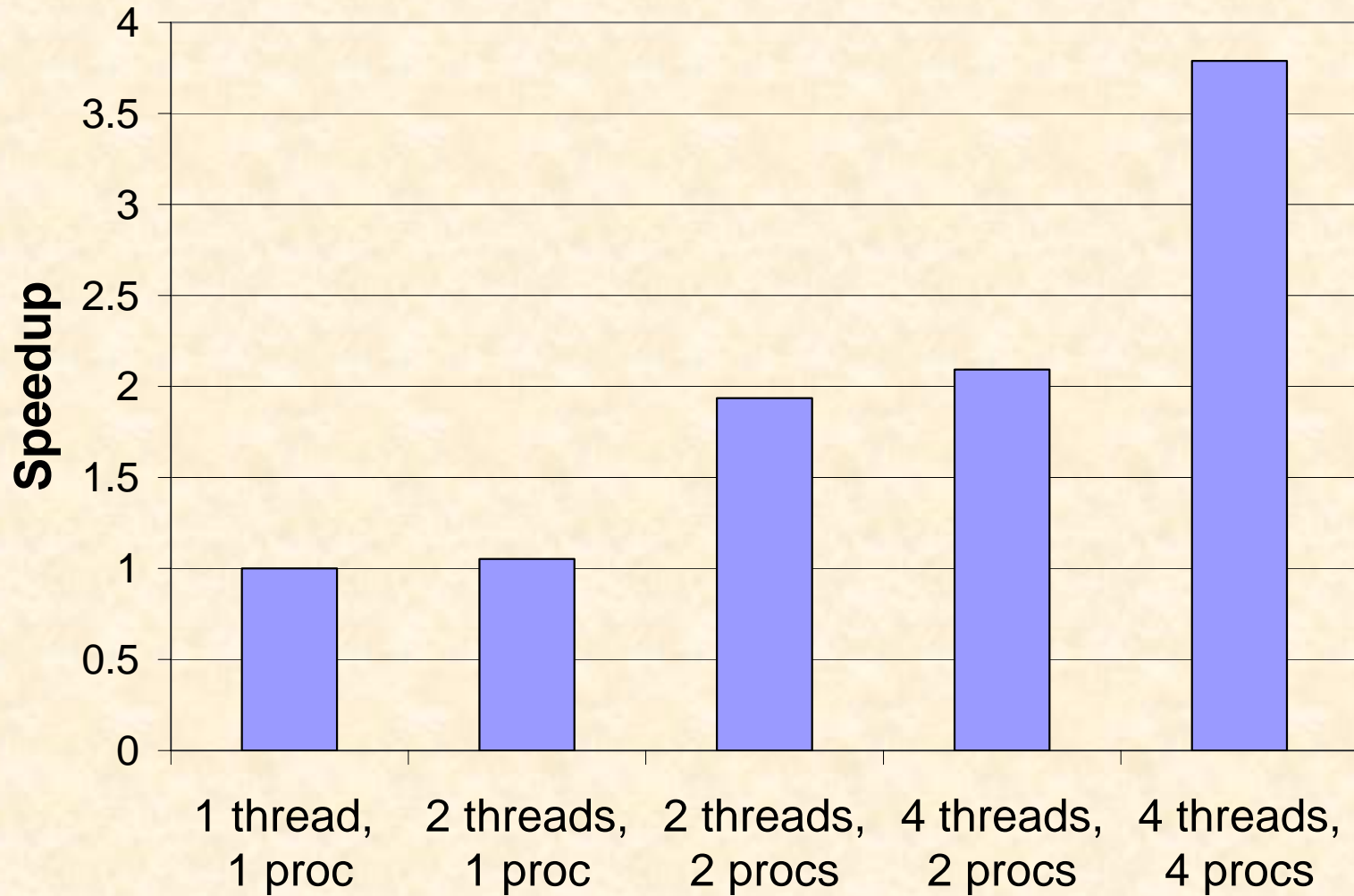
# Results

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- Full-Scale Simulation
    - Does not use Lookup Table
    - To avoid large messages, some inputs are read from disk
  - Execution Environment
    - 2.4 GHz Pentium IV processors w/ hyperthreading
    - 1 GB RAM each
    - 4 nodes
-

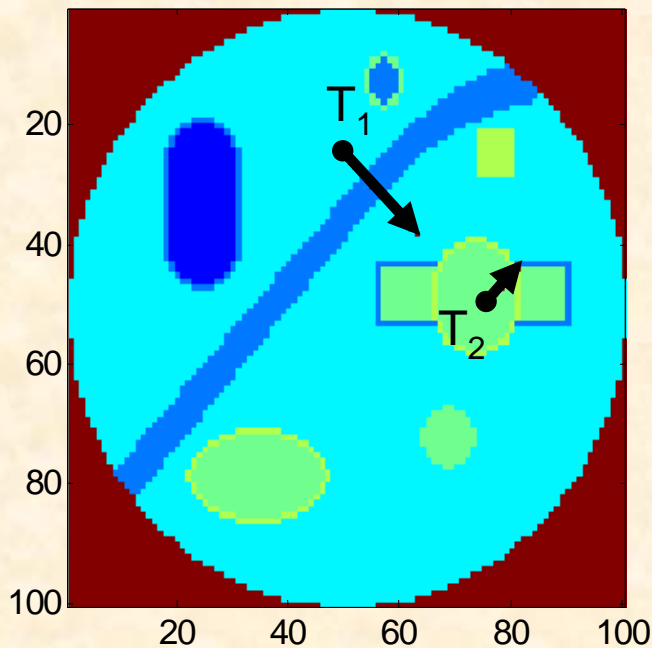


# Results



# Detection Example

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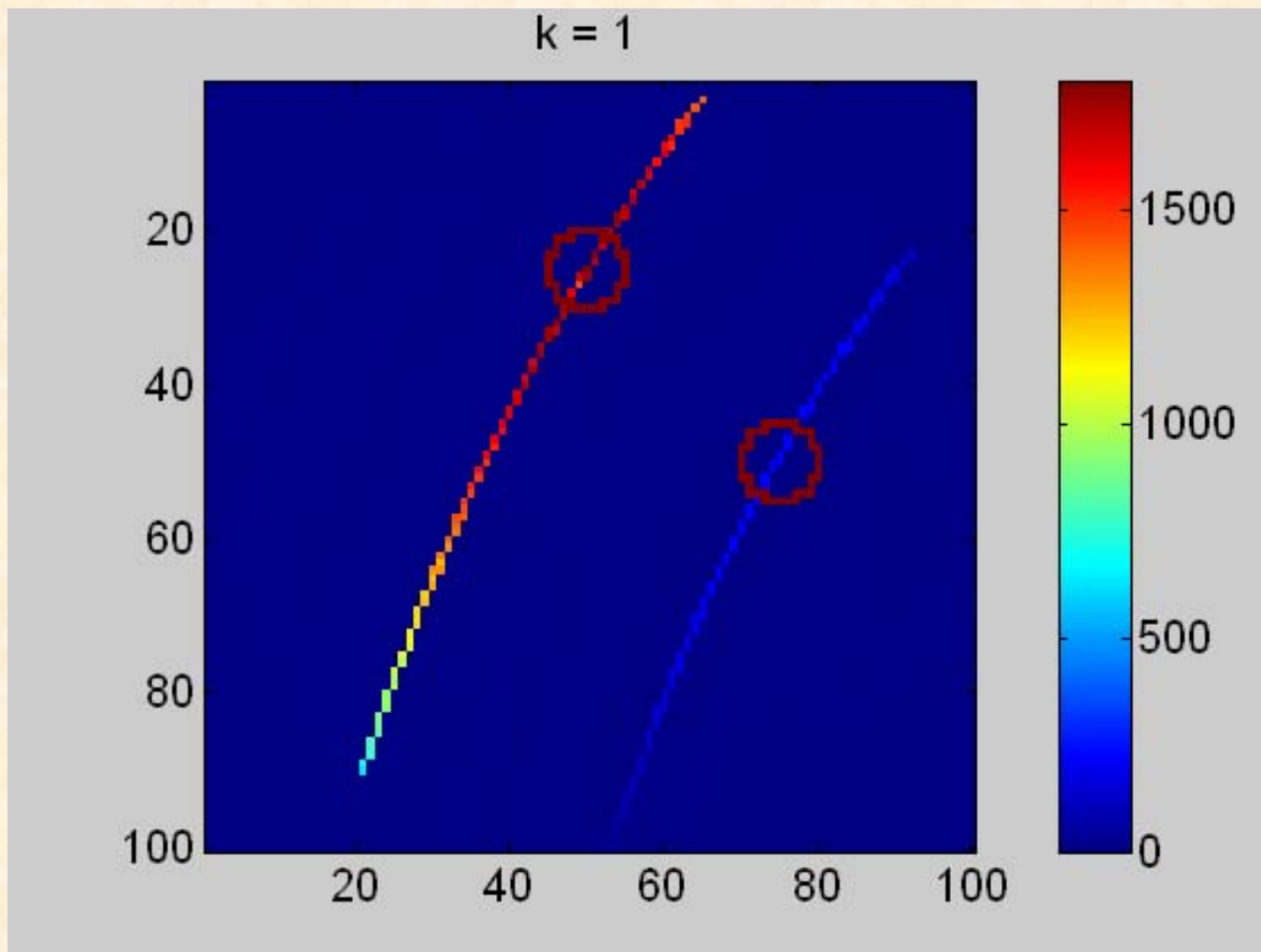
- Two artificial targets
- In small-scale environment
- Binary detection problem

$$\mathbf{z}_k = \begin{cases} \mathbf{s}_k + \mathbf{A}_k \mathbf{u}_k + \mathbf{n}_k & H_1 \\ \mathbf{A}_k \mathbf{u}_k + \mathbf{n}_k & H_0 \end{cases}$$

- Use adaptive matched filter
-

# Adaptive Matched Filter Detector

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# Current and Future Work

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- Completing the Full-Scale Simulation
    - Long runtimes are still a problem
  - Moving Target Estimation on Full-Scale System
-